

Lesson 9-6

Solving Quadratic Equations by Using the Quadratic Formula



The Quadratic Formula can be used to solve equations in the form of $ax^2 + bx + c = 0$, where $a \neq 0$. The quadratic formula is

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$Ax^2 + Bx + C = 0$$

A. Solve $x^2 - 2x - 35 = 0$ by using the Quadratic Formula.

$$a = 1, b = -2, c = -35$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Quadratic Formula

$$\frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(-35)}}{2(1)}$$

$$x = \frac{2 \pm \sqrt{4 + 140}}{2(1)}$$

Substitute

$$x = \frac{2}{2 \pm \sqrt{144}}$$

Multiply

$$x = \frac{2}{2}$$

Add

$$\frac{2 \pm 12}{2}$$

$$x = \frac{2}{2}$$

Simplify

$$x = \frac{2+12}{2} \quad x = \frac{2-12}{2}$$

Write 2 equations

$$x = \frac{14}{2} = 7 \quad x = \frac{-10}{2} = -5$$

$$\{7, -5\}$$

The solution set is

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Practice:

1. Solve $x^2 + x - 30 = 0$

$$a = 1, b = 1, c = -30$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-1 \pm \sqrt{1^2 - 4(1)(-30)}}{2(1)}$$

$$x = \frac{-1 \pm \sqrt{1+120}}{2}$$

$$x = \frac{-1 \pm \sqrt{121}}{2}$$

$$x = \frac{-1 \pm 11}{2}$$

$$x = \frac{-1+11}{2} \quad x = \frac{-1-11}{2}$$

$$x = \frac{10}{2} = 5 \quad x = \frac{-12}{2} = -6$$

The solution set is $\{5, -6\}$

2. Solve $x^2 + 7x + 6 = 0$

$$a = 1, b = 7, c = 6$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-7 \pm \sqrt{7^2 - 4(1)(6)}}{2(1)}$$

$$x = \frac{-7 \pm \sqrt{49-24}}{2}$$

$$x = \frac{-7 \pm \sqrt{25}}{2}$$

$$x = \frac{-7 \pm 5}{2}$$

$$x = \frac{-7+5}{2} \quad x = \frac{-7-5}{2}$$

$$x = \frac{-2}{2} = -1 \quad x = \frac{-12}{2} = -6$$

The solution set is $\{-1, -6\}$

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Irrational Roots

Solve $15x^2 - 8x = 4$ by using the Quadratic Formula. Round to the nearest tenth if necessary.

STEP 1 – Rewrite the equation in standard form.

$$\begin{array}{l} 15x^2 - 8x = 4 \\ 15x^2 - 8x - 4 = 4 - 4 \\ \hline 15x^2 - 8x - 4 = 0 \end{array}$$

Original equation.

Set equation equal to zero.

Simplify

STEP 2 – Apply the Quadratic Formula $a = 15 \quad b = -8 \quad c = -4$

$$\begin{aligned} x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-(-8) \pm \sqrt{(-8)^2 - 4(15)(-4)}}{2(15)} \\ x &= \frac{8 \pm \sqrt{64 + 240}}{30} \\ x &= \frac{8 \pm \sqrt{304}}{30} \\ x &= \frac{(8 + \sqrt{304})}{30} \quad x = \frac{8 - \sqrt{304}}{30} \end{aligned}$$

$$x = 0.85 \quad x = -0.31$$

The solution set is $\underline{\{0.85, -0.31\}}$

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Practice:

3. Solve $20x^2 - 4x = 8$

$$\begin{array}{l} a=20 \\ b=-4 \\ c=-8 \end{array}$$

$$20x^2 - 4x - 8 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(20)(-8)}}{2(20)}$$

$$x = \frac{4 \pm \sqrt{16 + 640}}{40}$$

$$x = \frac{4 \pm \sqrt{656}}{40}$$

$$x = \frac{(4 + \sqrt{656})}{40} \quad x = \frac{(4 - \sqrt{656})}{40}$$

$$x = 0.74$$

$$x = -0.54$$

4. Solve $4x^2 + 2x = 17$

$$\begin{array}{l} a=4 \\ b=2 \\ c=-17 \end{array}$$

$$4x^2 + 2x - 17 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-2 \pm \sqrt{2^2 - 4(4)(-17)}}{2(4)}$$

$$x = \frac{-2 \pm \sqrt{4 + 272}}{8}$$

$$x = \frac{-2 \pm \sqrt{276}}{8}$$

$$x = \frac{-2 + \sqrt{276}}{8} \text{ OR } x = \frac{-2 - \sqrt{276}}{8}$$

$$x = 1.83 \text{ OR } x = -2.33$$

① Write equation in standard form

② Identify $a, b, +c$.

③ APPS

④ - POLYSLMT

⑤ - POLYRoot Finder

ORDER = 2; DECIMAL
NEXT

⑥ enter A, B, +C
9-6 Using the Quadratic Formula

⑦ SOLVE

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In the Quadratic Formula, the expression under the radical sign, $b^2 - 4ac$, is called the discriminant. If the discriminant is positive, there are 2 real roots (answers) and the graph will cross the x-axis in two places, if the discriminant equals zero, there is 1 double root – (the graph touches the x-axis in 1 place), and if the discriminant is negative there are NO real roots (the graph does not cross the x-axis.)

Find the value of the discriminant. Then determine the number of real roots of the equation.

C. $\frac{A}{4}x^2 + \frac{B}{-2}x + \frac{C}{14} = 0$

$$\begin{aligned} b^2 - 4ac &= \underline{(-2)^2 - 4(4)(14)} \\ &= \underline{4 - 224 = -220} \end{aligned}$$

There are NO real roots.

D. $\frac{A}{x^2} + \frac{B}{24}x + \frac{C}{-144} = 0$

$$\begin{aligned} x^2 + 24x + 144 &= 0 \\ \cancel{x^2} & \end{aligned}$$

$$\begin{aligned} b^2 - 4ac &= \underline{24^2 - 4(1)(144)} \\ &= \underline{576 - 576 = 0} \end{aligned}$$

There are 1 real roots.

E. $\frac{A}{1}x^2 + \frac{B}{2}x + \frac{C}{2} = 0$

$$\begin{aligned} b^2 - 4ac &= \underline{2^2 - 4(1)(2)} \\ &= \underline{4 - 8 = -4} \end{aligned}$$

There are NO real roots.

F. $-5x^2 + 10x = -1$

$$\begin{aligned} \frac{-5x^2}{a} + \frac{10x}{b} + \frac{1}{c} &= 0 \end{aligned}$$

$$\begin{aligned} b^2 - 4ac &= \underline{10^2 + -4(-5)(1)} \\ &= \underline{100 + 20 = 120} \end{aligned}$$

There are 2 real roots.

COMPLETE AND TURN IN FOR A DAILY GRADE
 ① Write in standard form, ② Identify a, b, + c ③ Give the solution.

Solve using POLYSMUR APP

$$A) 0 = 2x^2 - 3x - 5$$

$$a = 2 \quad b = -3 \quad c = -5$$

$$\{2.5, -1\}$$

$$B) 2x + 10 = 4x^2$$

$$\frac{-4x^2}{-4x^2} \quad \frac{-4x^2}{-4x^2}$$

$$-4x^2 + 2x + 10 = 0$$

$$a = -4, b = 2, c = 10 \quad \{1.85, -1.35\}$$

$$*1) x^2 - 9 = 0 \quad 6) -3x^2 - 4x = -20$$

$$2) 5x^2 + 3x - 2 = 0 \quad 7) 4x^2 = 16$$

$$3) -2x^2 + 5x + 3 = 0 \quad *8) 10 - x^2 = 3x$$

$$4) -3x^2 + 15x = 0 \quad *9) -2x^2 + 6 = 4x$$

$$5) x^2 + 18x + 81 = 0 \quad *10) 3x^2 - 9 = -6x$$